# Far-from-equilibrium dynamics of molecules in <sup>4</sup>He nanodroplets: a quasiparticle perspective

Giacomo Bighin Institute of Science and Technology Austria

Spring (online) Workshop on Ultracold Quantum Matter — Padova, June 4th, 2020

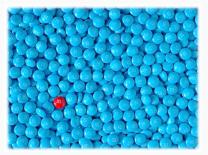
#### **Quantum impurities**

One particle (or a few particles) interacting with a many-body environment.

- Condensed matter
- Chemistry
- Ultracold atoms: tunable interaction with either bosons or fermions.

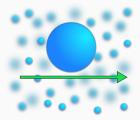
A prototype of a many-body system.

How are the properties of the particle modified by the interaction?





Most common cases: electron in a solid, atomic impurities in a BEC.



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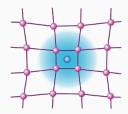


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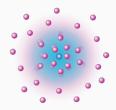


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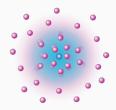
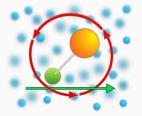


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**Composite impurity (e.g. a molecule):** translational *and rotational* degrees of freedom/linear and angular momentum exchange.

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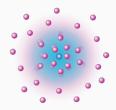
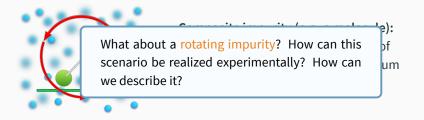


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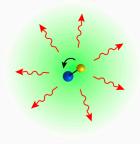


#### Composite impurities: where to find them



Strong motivation for the study of composite impurities comes from many different fields. Composite impurities can be realized as:

• Ultracold molecules and ions.



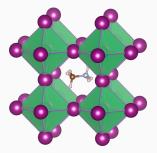
B. Midya, M. Tomza, R. Schmidt, and M. Lemeshko, Phys. Rev. A **94**, 041601(R) (2016).

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- Rotating molecules inside a 'cage' in perovskites.



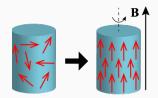
T. Chen et al., PNAS **114**, 7519 (2017). J. Lahnsteiner et al., Phys. Rev. B **94**, 214114 (2016). Image from: C. Eames et al, Nat. Comm. **6**, 7497 (2015).

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- Rotating molecules inside a 'cage' in perovskites.
- Angular momentum transfer from the electrons to a crystal lattice.



J.H. Mentink, M.I. Katsnelson, M. Lemeshko, "Quantum many-body dynamics of the Einstein-de Haas effect", Phys. Rev. B **99**, 064428 (2019).



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- Rotating molecules inside a 'cage' in perovskites.
- Angular momentum transfer from the electrons to a crystal lattice.
- Molecules embedded into helium nanodroplets.

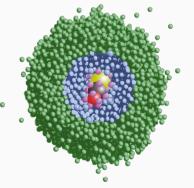


Image from: J. P. Toennies and A. F. Vilesov, Angew. Chem. Int. Ed. **43**, 2622 (2004).

# Molecules in helium nanodroplets

A molecular impurity embedded into a helium nanodroplet: a controllable system to explore angular momentum redistribution in a many-body environment.

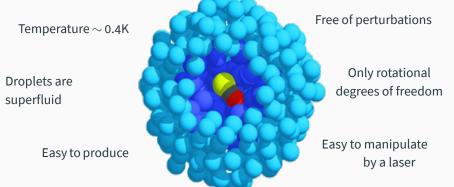
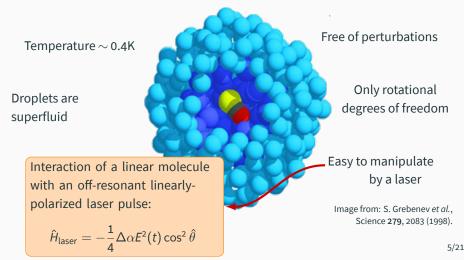


Image from: S. Grebenev *et al.*, Science **279**, 2083 (1998).

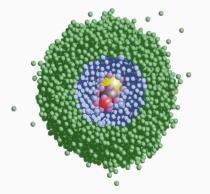
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#### Rotational spectrum of molecules in He nanodroplets

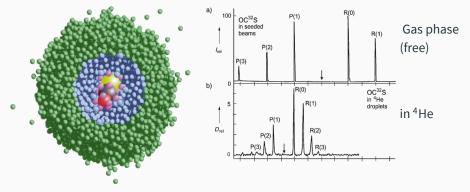
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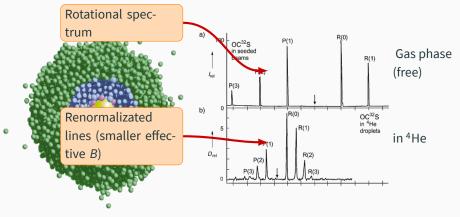
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# Dynamical alignment of molecules in He nanodroplets

**Dynamical alignment** experiments (Stapelfeldt group, Aarhus University):

- Kick pulse, aligning the molecule.
- Probe pulse, destroying the molecule.
- Fragments are imaged, reconstructing alignment as a function of time.
- Averaging over multiple realizations, and varying the time between the two pulses, one gets

$$\left\langle \cos^2 \hat{\theta}_{2\mathsf{D}} \right\rangle (t)$$

with:

$$\cos^2\hat{\theta}_{\rm 2D}\equiv \frac{\cos^2\hat{\theta}}{\cos^2\hat{\theta}+\sin^2\hat{\theta}\sin^2\hat{\phi}}$$

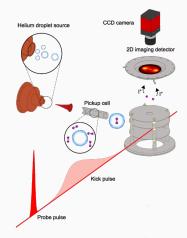
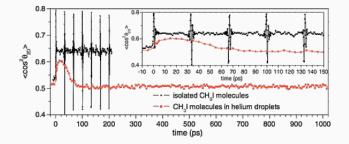


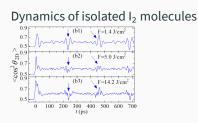
Image from: B. Shepperson *et al.*, Phys. Rev. Lett. **118**, 203203 (2017).

#### Effect of the environment is substantial: free molecule vs. same molecule in He.



Stapelfeldt group, Phys. Rev. Lett. 110, 093002 (2013).

# Dynamical alignment of molecules in He nanodroplets

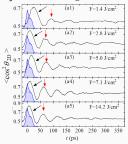


Experiment: Stapelfeldt group (Aarhus University).

#### Effect of the environment is substantial:

- The peak of prompt alignment doesn't change its shape as the fluence  $F = \int dt \, I(t)$  is changed.
- The revival structure differs from the gas-phase: revivals with a 50ps period of unknown origin.
- The oscillations appear weaker at higher fluences.
- An intriguing puzzle: not even a qualitative understanding. Monte Carlo? He-DFT?

#### Dynamics of I<sub>2</sub> molecules in helium



The quantum mechanical treatment of many-body systems is always challenging. How can one simplify the quantum impurity problem?

#### **Quasiparticle approach**

The quantum mechanical treatment of many-body systems is always challenging. How can one simplify the quantum impurity problem?

**Polaron**: an electron dressed by a field of many-body excitations.

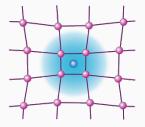
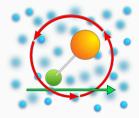


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**Angulon**: a quantum rotor dressed by a field of many-body excitations.



R. Schmidt and M. Lemeshko, Phys. Rev. Lett. **114**, 203001 (2015).

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#### The Hamiltonian

A rotating linear molecule interacting with a bosonic bath can be described in the frame co-rotating with the molecule by the following Hamiltonian:

$$\hat{\mathcal{H}} = B(\widehat{\mathbf{L}} - \hat{\Lambda})^2 + \sum_{k\lambda\mu} \omega_k \hat{b}^{\dagger}_{k\lambda\mu} \hat{b}_{k\lambda\mu} + \sum_{k\lambda} V_{k\lambda} (\hat{b}^{\dagger}_{k\lambda0} + \hat{b}_{k\lambda0}),$$

Notation:

- $\widehat{\mathbf{L}}$  the total angular-momentum operator of the combined system, consisting of a molecule and helium excitations.
- $\hat{\Lambda}$  is the angular-momentum operator for the bosonic helium bath, whose excitations are described by  $\hat{b}_{k\lambda\mu}/\hat{b}^{\dagger}_{k\lambda\mu}$  operators.
- $k\lambda\mu$ : angular momentum basis. k the magnitude of linear momentum of the boson,  $\lambda$  its angular momentum, and  $\mu$  the *z*-axis angular momentum projection.
- $\omega_k$  gives the dispersion relation of superfluid helium.
- $V_{k\lambda}$  encodes the details of the molecule-helium interactions.

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$$\hat{H}_{LLP} = \frac{\left(\mathbf{P} - \sum_{\mathbf{k}} \mathbf{k} \hat{b}_{\mathbf{k}}^{\dagger} \hat{b}_{\mathbf{k}}\right)^{2}}{2m_{l}} + \sum_{\mathbf{k}} \omega_{\mathbf{k}} \hat{b}_{\mathbf{k}}^{\dagger} \hat{b}_{\mathbf{k}} + \frac{g}{\mathcal{V}} \sum_{\mathbf{k}, \mathbf{k}'} \hat{b}_{\mathbf{k}'}^{\dagger} \hat{b}_{\mathbf{k}'} \quad \text{tions.}$$



We describe dynamics using a time-dependent variational Ansatz, including excitations up to one phonon:

$$\ket{\psi_{LM}(t)} = \hat{U}(\underline{g_{LM}(t)}\ket{0}_{\text{bos}}\ket{LM0} + \sum_{k\lambda n} \alpha_{k\lambda n}^{LM}(t) b_{k\lambda n}^{\dagger}\ket{0}_{\text{bos}}\ket{LMn})$$

Lagrangian on the variational manifold defined by  $|\psi_{LM}\rangle$ :

$$\mathcal{L} = \langle \psi_{LM} | i \partial_t - \hat{\mathcal{H}} | \psi_{LM} \rangle$$

Euler-Lagrange equations of motion:

$$\frac{d}{dt}\frac{\partial \mathcal{L}}{\partial \dot{x}_i} - \frac{\partial \mathcal{L}}{\partial x_i} = 0$$

where  $x_i = \{g_{LM}, \alpha_{k\lambda n}^{LM}\}$ . We obtain a differential system

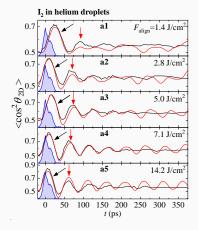
$$\begin{cases} \dot{g}_{LM}(t) = \dots \\ \dot{\alpha}_{k\lambda n}^{LM}(t) = \dots \end{cases}$$

to be solved numerically; in  $\alpha_{k\lambda\mu}$  the momentum *k* needs to be discretized.

#### Theory vs. experiments: I<sub>2</sub>



Comparison with experimental data from Stapelfeldt group, Aarhus University, for different molecules: I<sub>2</sub>.



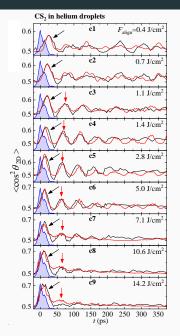
Generally good agreement for the main features in experimental data:

- Oscillations with a period of 50ps, growing in amplitude as the laser fluence is increased.
- Oscillations decay: at most 4 periods are visible.
- The width of the first peak does not change much with fluence.

Experiment
Angulon theory

Laser pulse

#### Theory vs. experiments: CS<sub>2</sub>



Comparison with experimental data from Stapelfeldt group, Aarhus University, for different molecules: CS<sub>2</sub>.



- Again, a persistent oscillatory pattern.
- For higher values of the fluence the oscillatory pattern disappears.

------ Experiment

Laser pulse

—— Angulon theory

• Can we shed light on the origin of oscillations? Why the 50ps period? Why do they sometimes disappear? What about the decay?



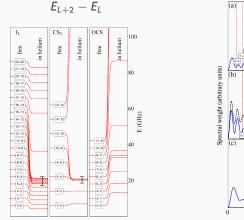
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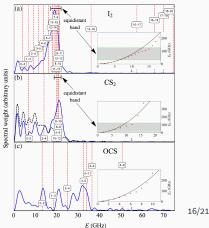


- A microscopical theory allows us to reconstruct the pathways of angular momentum redistribution: microscopical insight on the problem!
  - We can fully characterize the helium excitations dressing by the molecule.
  - At the same we can also analyze how molecular properties (populations, energy levels) are affected by the many-body environment.

#### Experiments vs. theory: spectrum

The Fourier transform of the measured alignment cosine  $\langle \cos^2 \hat{\theta}_{2D} \rangle(t)$  is dominated by  $(L) \leftrightarrow (L+2)$  interferences. How is it affected when the level structure changes?





#### Experiments vs. theory: spectrum

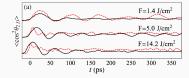
The Fourier transform of the measured alignment cosine  $\langle \cos^2 \hat{\theta}_{2D} \rangle(t)$  is dominated by  $(L) \leftrightarrow (L+2)$  interferences. How is it affected when the level structure changes? 20Ghz corresponds to 50ps  $E_{L+2} - E_L$ Ь equidistant band  $I_2$  $CS_2$ OCS 100 in helium n helium n helium free free free 22-20 Spectral weight (arbitrary units) 80 (b)20-18 CS<sub>2</sub> 19-17 equidistant band 16-14 16-14 60 15-13 E (GHz) 14-12 100 🗟 13-11 20 11-9 (c) OCS 10-8 -(10+8) 9-7 8-6 -8-6 8.6 6-4 6-4 -5-3 0 10 20 30 40 50 60 70

16/21

E (GHz)

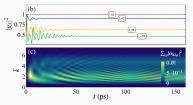
#### Many-body dynamics of angular momentum

i) Is this the full story? Can the observed dynamics be explained only by means of renormalised rotational levels?



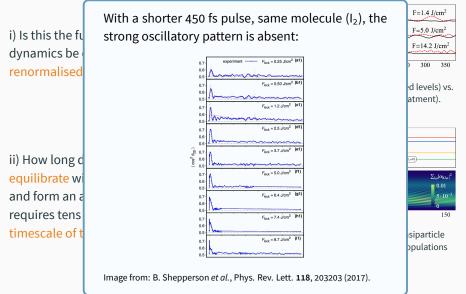
Red dashed lines (only renormalised levels) vs. solid black line (full many-body treatment).

ii) How long does it take for a molecule to equilibrate with the helium environment and form an angulon quasiparticle? This requires tens of ps; which is also the timescale of the laser!



Approach to equilibrium of the quasiparticle weight  $|g_{LM}|^2$  and of the phonon populations  $\sum_k |\alpha_{k\lambda\mu}|^2$ .

#### Many-body dynamics of angular momentum



#### Conclusions

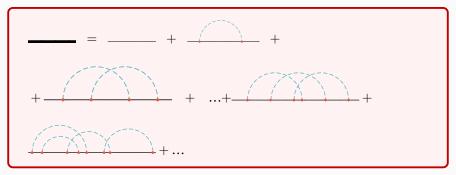
- A novel kind of pump-probe spectroscopy, based on impulsive molecular alignment in the laboratory frame, providing access to the structure of highly excited rotational states.
- Robust long-wavelength oscillations in the molecular alignment, whose explanation requires a many-body theory of angular momentum.
- Our theoretical model allows us to interpret this behavior in terms of the dynamics of angulon quasiparticles, shedding light onto many-particle dynamics of angular momentum at femtosecond timescales.
- Future perspectives:
  - All molecular geometries (spherical tops, asymmetric tops).
  - Optical centrifuges and superrotors.
  - Can a rotating molecule create a vortex?
- For more details: arXiv:1906.12238. See also A.S. Chatterley,

L. Christiansen, C.A. Schouder, A.V. Jørgensen, B. Shepperson,

I.N. Cherepanov, GB, R.E. Zillich, M. Lemeshko, H. Stapelfeldt, *"Rotational coherence spectroscopy of molecules in helium nanodroplets: Reconciling the time and the frequency domains"*, Phys. Rev. Lett., in press. 18/21

#### Diagrammatic Monte Carlo

More numerical approach: **DiagMC**, sampling all diagrams in a stochastic way.



How do we describe angular momentum redistribution in terms of diagrams? How does the configuration space looks like?

Can we use DiagMC to describe a molecule?

GB and M. Lemeshko, Phys. Rev. B **96**, 419 (2017). GB, T.V. Tscherbul, M. Lemeshko, Phys. Rev. Lett. **121**, 165301 (2018). Lemeshko group @ IST Austria:

Misha Lemeshko



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Enderalp Yakabovlu



Xiang Li

Collaborators:



Henrik Stapelfeldt (Aarhus)



Richard Schmidt (MPO



Timur Tscherbul 20/21 (Reno)











Dynamics in He

Wojciech Rzadkowski



Cherepanov

# Thank you for your attention.



Der Wissenschaftsfonds.

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These slides at http://bigh.in

#### Backup slide # 1: finite-temperature dynamics

For the impurity: average over a statistical ensamble, weights  $\propto \exp(-\beta E_L)$ .

For the bath: the zero-temperature bosonic expectation values in  $\mathcal{L}$  are converted to finite temperature ones<sup>1,2</sup>.

$$\mathcal{L}_{\mathcal{T}=0} = \langle 0 | \hat{O}^{\dagger}(\mathrm{i}\partial_{t} - \hat{\mathcal{H}}) \hat{O} | 0 \rangle_{\mathsf{bos}} \longrightarrow \mathcal{L}_{\mathcal{T}} = \mathsf{Tr} \Big[ \rho_{0} \, \hat{O}^{\dagger}(\mathrm{i}\partial_{t} - \hat{\mathcal{H}}) \hat{O} \Big]$$

[1] A. R. DeAngelis and G. Gatoff, Phys. Rev. C 43, 2747 (1991).

[2] W.E. Liu, J. Levinsen, M. M. Parish, "Variational approach for impurity dynamics at finite temperature", arXiv:1805.10013

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A couple of additional details:

- The laser changes the total angular momentum of the system. An appropriate wavefunction is then  $|\Psi\rangle = \sum_{LM} |\psi_{LM}\rangle$
- Focal averaging, accounting for the fact that the laser is not always perfectly focused.
- States with odd/even angular momenta may have different abundances, due to the nuclear spin.

[1] A. R. DeAngelis and G. Gatoff, Phys. Rev. C 43, 2747 (1991).

[2] W.E. Liu, J. Levinsen, M. M. Parish, "Variational approach for impurity dynamics at finite temperature", arXiv:1805.10013

#### Backup slide # 2: the angulon

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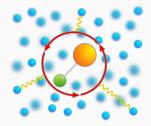
A composite impurity in a bosonic environment can be described by the angulon Hamiltonian<sup>1,2,3,4</sup> (angular momentum basis:  $\mathbf{k} \rightarrow \{k, \lambda, \mu\}$ ):

$$\hat{H} = \underbrace{B\hat{\mathbf{J}}^{2}}_{\text{molecule}} + \underbrace{\sum_{k\lambda\mu} \omega_{k} \hat{b}^{\dagger}_{k\lambda\mu} \hat{b}_{k\lambda\mu}}_{\text{phonons}} + \underbrace{\sum_{k\lambda\mu} U_{\lambda}(k) \left[Y^{*}_{\lambda\mu}(\hat{\theta}, \hat{\phi}) \hat{b}^{\dagger}_{k\lambda\mu} + Y_{\lambda\mu}(\hat{\theta}, \hat{\phi}) \hat{b}_{k\lambda\mu}\right]}_{\text{molecule-phonon interaction}}$$

- Linear molecule.
- Derived rigorously for a molecule in a weakly-interacting BEC<sup>1</sup>.
- Phenomenological model for a molecule in any kind of bosonic bath<sup>3</sup>.

<sup>1</sup>R. Schmidt and M. Lemeshko, Phys. Rev. Lett. **114**, 203001 (2015).

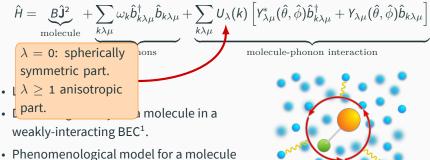
- <sup>2</sup>R. Schmidt and M. Lemeshko, Phys. Rev. X 6, 011012 (2016).
- <sup>3</sup>M. Lemeshko, Phys. Rev. Lett. **118**, 095301 (2017).
- <sup>4</sup>Yu. Shchadilova, "Viewpoint: A New Angle on Quantum Impurities", Physics 10, 20 (2017).



#### Backup slide # 2: the angulon



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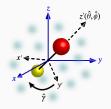
#### Backup slide # 3: canonical transformation

We apply a canonical transformation

 $\hat{S} = e^{-\mathrm{i}\hat{\phi}\otimes\hat{\Lambda}_z} e^{-\mathrm{i}\hat{\theta}\otimes\hat{\Lambda}_y} e^{-\mathrm{i}\hat{\gamma}\otimes\hat{\Lambda}_z}$ 

where  $\hat{\Lambda} = \sum_{\mu\nu} b^{\dagger}_{k\lambda\mu} \vec{\sigma}_{\mu\nu} b_{k\lambda\nu}$  is the angular momentum of the bosons.

Cfr. the Lee-Low-Pines transformation for the polaron.



**Bosons:** laboratory frame (x, y, z)**Molecule:** rotating frame (x', y', z')defined by the Euler angles  $(\hat{\phi}, \hat{\theta}, \hat{\gamma})$ .

